

5.6 Graphing Rational Functions

$$1) f(x) = \frac{1}{3x^2+3x-18} = \frac{1}{3(x^2+x-6)} = \frac{1}{3(x+3)(x-2)}$$

VA: $x=-3, x=2$ Holes: none HA: $y=0$

X-int: none

$$2) f(x) = \frac{x-2}{x-4} \quad \text{VA: } x=4 \quad \text{Holes: none} \quad \text{HA: } y=1$$

X-int: 2

$$3) f(x) = \frac{x^3-x^2-6x}{-3x^2-3x+18} = \frac{x(x^2-x-6)}{-3(x^2+x+6)} = \frac{x(x-3)(x+2)}{-3(x^2+x+6)} \leftarrow \text{doesn't factor}$$

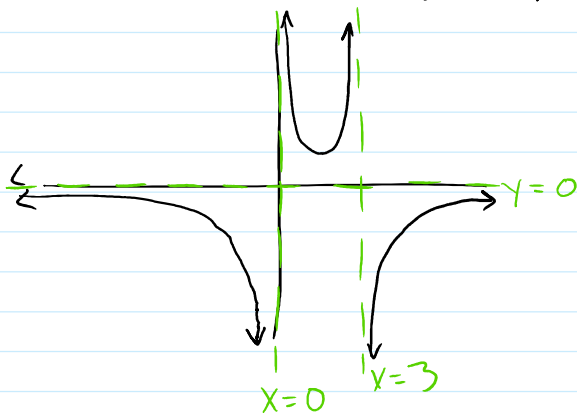
VA: none HA: none Holes: none X-int: 0, 3, -2

$$4) f(x) = \frac{x^2+x-6}{-4x^2-16x-12} = \frac{(x-2)(x+3)}{-4(x^2+4x+3)} = \frac{(x-2)(x+3)}{-4(x+3)(x+1)} = \frac{x-2}{4(x+1)}$$

VA: $x=-1$ HA: $y=-1/4$ Hole: $x=-3$ X-int: 2

$$5) f(x) = -\frac{4}{x^2-3x} = -\frac{4}{x(x-3)} \quad \text{VA: } x=0, x=3 \quad \text{HA: } y=0$$

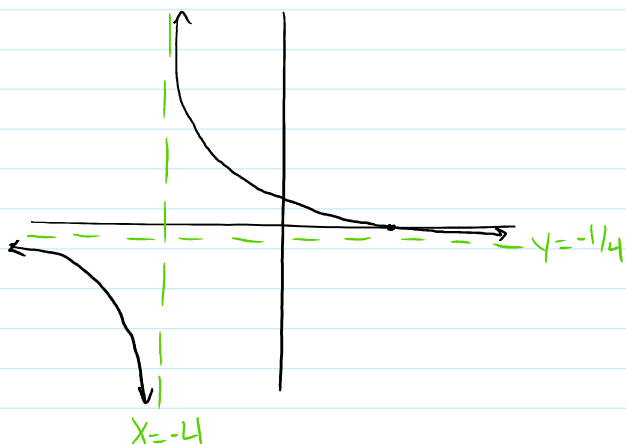
X-int: none Hole: none



$$6) f(x) = \frac{x-4}{x-4} \quad \text{VA: } x=-4 \quad \text{HA: } y=-1/4 \quad \text{Hole: none}$$

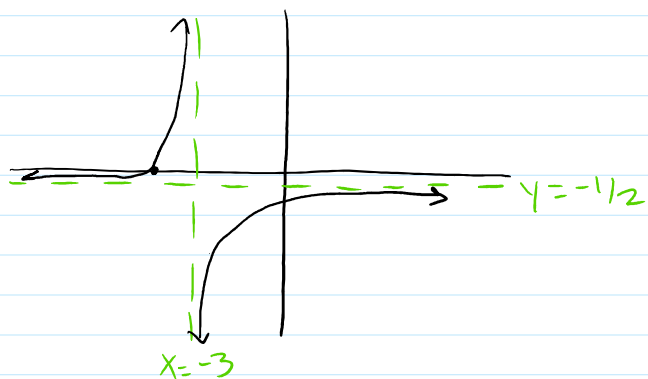
$$6) f(x) = \frac{x-4}{-4x-16} = \frac{x-4}{-4(x+4)}$$

$$\text{VA: } x = -4 \quad \text{HA: } y = -1/4 \quad \text{Hole: none} \\ \text{x-int: } 4$$



$$7) f(x) = \frac{x+4}{-2x-6} = \frac{x+4}{-2(x+3)}$$

$$\text{VA: } x = -3 \quad \text{HA: } -1/2 \quad \text{Hole: none} \\ \text{x-int: } -4$$



$$8) f(x) = \frac{x^3 - 9x}{3x^2 - 6x - 9} = \frac{x(x^2 - 9)}{3(x^2 - 2x - 3)} = \frac{x(x-3)(x+3)}{3(x-3)(x+1)} = \frac{x(x+3)}{3(x+1)}$$

$$\text{VA: } x = -1 \quad \text{HA: none} \quad \text{Hole: } x = 3 \quad \text{x-int: } x = -3, 0$$

