Lesson 2.1: How Did I Do?


How well did you do on the Chapter 1 Test? How well did you do relative to your classmates?
Here are the results of a random sample of 20 of the Chapter 1 Tests, along with a dotplot and summary statistics.

| Test Scores | 61 | 65 | 65 | 73 | 75 | 77 | 78 | 78 | 79 | 80 | 80 | 80 | 80 | 81 | 81 | 88 | 89 | 93 | 98 | 99 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |



1. Biff scored a 65 . What is Biff's percentile?
2. Was Biff above or below the mean? By how many points? By how many standard deviations?
3. Marty scored an 88. What is Marty's percentile?
4. Was Marty above or below the mean? By how many points? By how many standard deviations?

A z-score is defined as the number of standard deviations above or below the mean.
5. Write a formula for calculating a z-score. $z=$
6. Goldie scored a 98 on the Chapter 1 Test. Find and interpret the z-score.

Bonus: Goldie was aspiring for what job?

There are two mathematical operations involved in calculating a z-score: $z=\frac{V A L U E-M E A N}{S D}$

1. First, we take each score, and $\qquad$ the mean (remember the mean was 80). Fill in the table and then make a dotplot for each.

| SCORE | 61 | 65 | 65 | 73 | 75 | 77 | 78 | 78 | 79 | 80 | 80 | 80 | 80 | 81 | 81 | 88 | 89 | 93 | 98 | 99 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| SCORE - MEAN |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

Dotplot for SCORE
Dotplot for SCORE - MEAN


What happens to the shape, center, and variability when you subtract the mean from each score?
2. Second, we take the SCORE - MEAN and $\qquad$ by the standard deviation (remember the standard deviation is 10). Fill in the table and then make a dotplot for each.

| SCORE - MEAN | -19 | -15 | -15 | -7 | -5 | -3 | -2 | -2 | -1 | 0 | 0 | 0 | 0 | 1 | 1 | 8 | 9 | 13 | 18 | 19 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SCORE - MEAN |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| SD |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

Dotplot for $\frac{\text { SCORE - MEAN }}{S D}$


What happens to the shape, center, and variability when you divide by the standard deviation for each value?

Let's summarize:
If you are given a list of data and you add or subtract the same value a from each value: Shape $\qquad$ Center $\qquad$ Variability: $\qquad$
If you are given a list of data and you multiply or divide by the same value $\mathbf{b}$ from each value:
Shape $\qquad$ Center $\qquad$ Variability: $\qquad$

The Chapter 1 Test scores have a mean of $\qquad$ and a standard deviation of $\qquad$ .

The z-scores of the Test scores have a mean of $\qquad$ and a standard deviation of $\qquad$ .

# Lesson 2.1 - Describing Location in a Distribution 

Big Ideas:

## Check Your Understanding:

Knoebels Amusement Park in Elysburg, Pennsylvania, has earned acclaim for being an affordable, family-friendly entertainment venue. Knoebels does not charge for general admission or parking, but it does charge customers for each ride they take. How much do the rides cost at Knoebels? The figure shows a dot- plot of the cost for each of 22 rides in a recent year, along with summary statistics.


Cost (\$)

1. Suppose you convert the cost of the rides from dollars to cents ( $\$ 1=100$ cents). Describe the shape, mean, and standard deviation of the distribution of ride cost in cents.
2. Knoebels' managers decide to increase the cost of each ride by 25 cents. How would this the shape, center, and variability of this distribution compare with the distribution of cost in Question 1?
3. Now suppose you convert the increased costs from Question 2 to $z$-scores. What would be the shape, mean, and standard deviation of this distribution? Explain your answers.

Homework: Pg 106 -- 15, 19, 21, 25, 29, 33-38

