One-Sample t Tests

1. When working properly, a soda machine will dispense soda with a mean of $\mu = 12$ ounces. A quality control engineer is concerned that the machine is over filling the cups. He draws a random sample of 8 cups and records the following amounts:

11.88

12.65

12.49

12.14

12.25

12.55

12.08

11.78

Is there evidence at the 5% level that the machine is over filling the cups?

P: State what the **parameter** of interest is representing in this problem.

H: State hypotheses in words and symbols.

A: Verify the assumptions/conditions.

- Random.
- Normal.
- Independent.

N: *Name* the appropriate inference procedure.

T: Carry out the selected procedure. Find the **test statistic**.

$$t = \frac{\bar{x} - \mu_0}{s / \sqrt{n}}$$

O: *Obtain* the corresponding P-value based on the test statistic and H_a .

M: *Make* a decision to reject or fail to reject H_0 .

S: *State* your conclusion in the context of the problem.

2. A hospital nurse is conducting a study about sleeping habits of four-year-olds. She wonders if they get more sleep than the recommended 8 hours per night. To test her claim, she collects a simple random sample of 12 four-year-olds and asks their parents how much sleep they got last night. Suppose the distribution of the amount of sleep for all four-year-olds is approximately Normal. The results are given below.

| Child | Hrs of sleep |
|-------|--------------|
| 1 | 9.25 |
| 2 | 8.25 |
| 3 | 6.50 |
| 4 | 8.50 |
| 5 | 7.50 |
| 6 | 9.25 |
| 7 | 9.00 |
| 8 | 8.00 |
| 9 | 8.25 |
| 10 | 9.75 |
| 11 | 10.00 |
| 12 | 9.25 |

Conduct an appropriate test of significance (at the 10% level) to decide if the data support the nurse's claim that four-year-olds average more than 8 hours of sleep per night.