

**\*\* Please sure to know ALL the properties for your test!**

**Geometric Properties**

Solve for x.

<p>1.</p> <p><math>2x+30 = x+80</math> <math>x = 50</math></p>	<p>2.</p> <p><math>3x+42 + 5x-22 = 180</math> <math>8x+20 = 180</math> <math>8x = 160</math> <math>x = 20</math></p>	<p>3.</p> <p><math>80 + 5x = 180</math> <math>5x = 100</math> <math>x = 20</math></p>
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**Proofs with Lines and Triangles**

<p>4. Given: <math>a \parallel b</math> and <math>c \parallel d</math> Prove: <math>\angle 1 \cong \angle 16</math></p>	<p>5. Given: C is the midpoint of <math>\overline{BE}</math>, <math>\angle A \cong \angle D</math> Prove: <math>\triangle ABC \cong \triangle DEC</math></p>
<p>1. <math>a \parallel b \implies c \parallel d</math> 2. <math>\angle 1 \cong \angle 5</math> 3. <math>\angle 5 \cong \angle 10</math> 4. <math>\angle 1 \cong \angle 10</math></p>	<p>1. Given 2. corresponding angles 3. Alternate exterior angles 4. Transitive property</p>
<p>1. C is the midpt of <math>\overline{BE}</math> 2. <math>\overline{AC} \cong \overline{CE}</math> 3. <math>\angle A \cong \angle D</math> 4. <math>\angle BCA \cong \angle DCE</math> 5. <math>\triangle ABC \cong \triangle DEC</math></p>	<p>1. Given 2. Def of midpt. 3. Given 4. Vertical <math>\angle</math>'s 5. ASA</p>

<p>6. Given: <math>\overline{BC} \cong \overline{DA}</math>, <math>\overline{BC} \parallel \overline{DA}</math> Prove: <math>\triangle ABC \cong \triangle CDA</math></p>	<p>7. Given: <math>\overline{BD} \perp \overline{AC}</math>, <math>\overline{BA} \cong \overline{BC}</math> Prove: <math>\triangle BAD \cong \triangle BCD</math></p>
<p>1. <math>\overline{BC} \cong \overline{DA}</math> 2. <math>\overline{BC} \parallel \overline{DA}</math> 3. <math>\angle CAD \cong \angle BCA</math> 4. <math>\overline{AC} \cong \overline{AC}</math> 5. <math>\triangle ABC \cong \triangle CDA</math></p>	<p>1. Given 2. Given 3. Alternate Int. <math>\angle</math>'s 4. Reflexive 5. SAS</p>
<p>1. <math>\overline{BD} \perp \overline{AC}</math> 2. <math>\angle BDA = 90^\circ</math> <math>\angle BDC = 90^\circ</math> 3. <math>\overline{BA} \cong \overline{BC}</math> 4. <math>\overline{BD} \cong \overline{BD}</math> 5. <math>\triangle BAD \cong \triangle BCD</math></p>	<p>1. Given 2. Def. of <math>\perp</math> lines 3. Given 4. Reflexive property 5. HL</p>

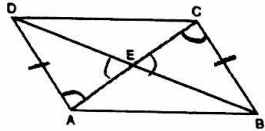
**Properties of Parallelograms**

Solve for x.

<p>8.</p> <p><math>2x+15 + x = 180</math> <math>3x+15 = 180</math> <math>3x = 165</math> <math>x = 55</math></p>	<p>9.</p> <p><math>5x-22 = 2x+35</math> <math>3x = 57</math> <math>x = 19</math></p>
<p>10.</p> <p><math>3x-8 = 2x+1</math> <math>x = 9</math></p>	<p>11. <math>BD = 8x+4</math> and <math>BE = 22</math></p> <p><math>8x+4 = 2(22)</math> <math>8x+4 = 44</math> <math>x = 5</math></p>

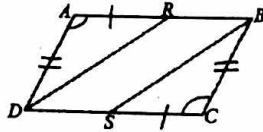
**Proofs with Parallelograms**

12. Given: ABCD is a parallelogram  
Prove:  $\triangle DEA \cong \triangle BEC$



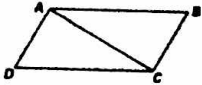
Statement:	Reason:
1. ABCD is a parallelogram	1. Given
2. $\overline{DA} \cong \overline{CB}$	2. Def of parallelogram
3. $\angle DAC \cong \angle BCA$	3. Alt. Int. Angles
4. $\angle AED \cong \angle BEC$	4. Vertical angles
5. $\triangle DEA \cong \triangle BEC$	5. SAA

13. Given: ABCD is a parallelogram,  $\overline{AR} \cong \overline{CS}$   
Prove:  $\triangle ARD \cong \triangle CSB$



Statement:	Reason:
1. ABCD is a parallelogram	1. Given
2. $\overline{AR} \cong \overline{CS}$	2. Given
3. $\overline{AD} \cong \overline{BC}$	3. Def of parallelogram
4. $\angle DAB \cong \angle BCD$	4. Def of parallelogram
5. $\triangle ARD \cong \triangle CSB$	5. SAS

14. Given: ABCD is a parallelogram  
Prove:  $\angle DAC \cong \angle BCA$

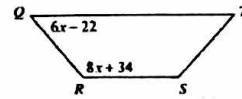


Statement:	Reason:
1. ABCD is a parallelogram	1. Given
2. $\overline{AB} \parallel \overline{DC}$	2. Def of parallelogram
3. $\angle DAC \cong \angle BCA$	3. Alt. Int. $\angle$ 's

**Properties of Quadrilaterals**

Solve for x (and y, if needed).

15. QTSR is a trapezoid.



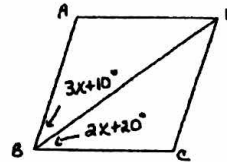
$$6x - 22 + 8x + 34 = 180$$

$$14x + 12 = 180$$

$$14x = 168$$

$$x = 12$$

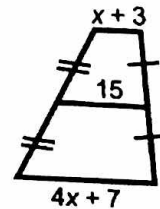
17. ABCD is a rhombus.



$$3x + 10 = 2x + 20$$

$$x = 10$$

19. Figure is a trapezoid.



$$15 = \frac{1}{2}(x+3+4x+7)$$

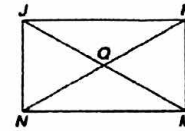
$$15 = \frac{1}{2}(5x+10)$$

$$15 = \frac{5}{2}x + 5$$

$$\left(\frac{2}{5}\right) 10 = \frac{2}{5} \left(\frac{5}{2}x + 5\right)$$

$$4 = x$$

16. KMNJ is a rectangle.  $KN = 3x + 14$  and  $JM = 38$

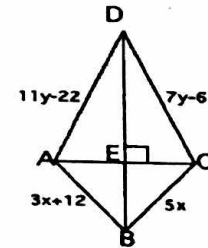


$$3x + 14 = 38$$

$$3x = 24$$

$$x = 8$$

18. ABCD is a kite.



$$11y - 22 = 7y - 6$$

$$\frac{4y}{4} = \frac{16}{4}$$

$$y = 4$$

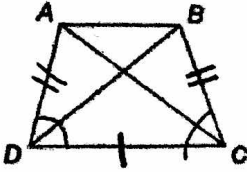
$$5x = 3x + 12$$

$$\frac{2x}{2} = \frac{12}{2}$$

$$x = 6$$

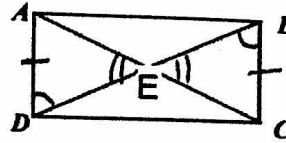
**Proofs with Quadrilaterals**

20. Given: ABCD is an isosceles trapezoid  
 Prove:  $\triangle ADC \cong \triangle BCD$



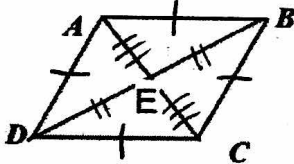
Statement:	Reason:
1. ABCD is an isosceles trapezoid	1. Given
2. $\angle ADC \cong \angle BCD$	2. Def of Isosceles Trapezoid
3. $\overline{DC} \cong \overline{DC}$	3. Reflexive
4. $\overline{AD} \cong \overline{BC}$	4. Legs of an isosceles trapezoid are congruent
5. $\triangle ADC \cong \triangle BCD$	5. SAS

21. Given: ABCD is a rectangle  
 Prove:  $\triangle ADE \cong \triangle BCE$



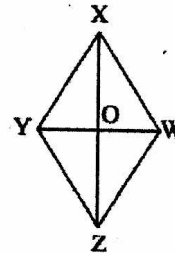
Statement:	Reason:
1. ABCD is a rectangle	1. Given
2. $\overline{AD} \cong \overline{BC}$	2. Def of a rect.
3. $\overline{AB} \parallel \overline{DC}$	3. Def. of a rect.
4. $\angle ADE \cong \angle BCE$	4. Alt. Int. $\angle$ 's
5. $\angle AED \cong \angle BEC$	5. Vertical $\angle$ 's
6. $\triangle ADE \cong \triangle BCE$	6. SAA

22. Given: ABCD is a rhombus  
 Prove:  $\triangle DEC \cong \triangle BEC$



Statement:	Reason:
1. ABCD is a rhombus	1. Given
2. $\overline{DC} \cong \overline{BC}$	2. Def. of rhombus
3. $\overline{ED} \cong \overline{BE}$ , $\overline{EC} \cong \overline{EC}$	3. Diagonals bisect each other.
4. $\triangle DEC \cong \triangle BEC$	4. SSS

23. Given:  $\overline{YX} \cong \overline{WX}$ ,  $\overline{ZX}$  bisects  $\angle YXW$   
 Prove:  $\overline{YO} \cong \overline{WO}$



Statement:	Reason:
1. $\overline{YX} \cong \overline{WX}$ , $\overline{ZX}$ bisects $\angle YXW$	1. Given
2. $\angle YXO \cong \angle WXZ$	2. Definition of bisect
3. $\overline{XO} \cong \overline{XO}$	3. Reflexive Property
4. $\triangle YXO \cong \triangle WXO$	4. SAS
5. $\overline{YO} \cong \overline{WO}$	5. CPCTC

Better name:  $\triangle WXO$